**Купавский Андрей Борисович Семейства множеств с запрещенными конфигурациями и приложения к дискретной геометрии независимости / Families of Sets With Forbidden Configurations and Applications to Discrete Geometry**

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