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## Изомонодромные деформации и квантовая теория поля = Isomonodromic deformations and quantum field theory : Isomonodromic deformations and quantum field theory : диссертация ... кандидата физико-математических наук : 01.01.00 / Гавриленко Павел Георгиевич ; [Место защиты: Нац. исслед. ун-т "Высшая школа экономики"]. - Москва, 2018. - 211 с. : ил.

## Оглавление диссертациикандидат наук Гавриленко Павел Георгиевич

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